Chapter IV:

The Complementarity of Classical and Statistical Investigations.

A review of the main points that have been made will prove, perhaps, the most expeditious introduction to the problem of the present chapter.

Our study of human intelligence began from an account of the psychological aspects of insight. It turned to geometrical definitions as products of insight and thence to the re-definitions that result from higher view-points. The argument that then twisted to the queer type of insight that consists in which grasping that the understanding of given data or of the answer to a given question consists in understanding that there is nothing to be understood. Finally, from an examination of infigures and of limits, there was effected the answer aligned a generalization that acknowledged in all data an empirical residue from which intelligence always abstracts.

The second chapter switched to insights in the field of smpri empirical science. After a brief contrast between mathematical and scientific developments of understanding, attention centered on the origin of the clues that form the first moment of insight. It was seen that, by inquiring, intelligence anticipates the act of understanding for which it strives. The concent of that anticipated act can be designated heuristically. The properties of the anticipated and designated content constitute the clues intellience employs to discovery guide itself towards discovery. Finally, since there are not only direct insights that understand what is to be understood but also the queer type of insights that understand that there is nothing to be understood, hearsztiz heuristic structures fall into two groups, namely, the classical and the statistical. A classical heuristic structure is intelligent anticipation of the systematic-and-abstract. A suatistical heuristic structure is intelligent anticipation of the systematic-and-abstract setting a boundary or norm from which the concrete cannot systematically diverge.

Of themselves, heuristic structures are empty. They anticipate a form that is to be filled. Now just as the form can be anticipated; in its general properties, so also can the process of filling be anticipated in its general properties. There exist, then, canons of empirical method. If insight is to be into data, there is a canon of selection. If insights into data results accumulate in a circuit of presentations, insights, formulations, experiments, new presentations, there is a canon of operations. If applied science involves insights into meterials, purposes, agents

science involves insights into materials, purposes, agents, and tools, then pure science, as prior to applied, will be concerned des solely with the immanent intelligibility of data and so will be subject to a canon of relevance. If pure science

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goes beyond the data in a smuch as it grasps their immanent intelligibility, still it adds to the data no more than that intelligible content; there results a canon of parsimony, which excludes any affirmation that goes beyond what can be verified in the data. If some data are to be understood, then all are to be understood; the scientific roal is the understanding of all phenomena, and so sc\_entific method is subject to a canon faxes of complete explanation; it follows that no exception is to be made for experienced extensions or for experienced durations; and this conclusion implies a shift from a Galilean to an Einsteinian viewpoint. Finally, though all data are to be axpiana explained, it remains that certain aspects of all data are explained in the queer fashion al ready noticed. There exists statistical residues, for the totality of the systematic is abstract, the abstract is applied to the concrete only by the addition of further determinations and, from the natu e of the case, the further determinations cannot be systematically related to one another.

Now this bare enumeration of the points aixe that have been made in our first three chapters confronts us with a problem. Both the heuristic structures of science and the canons of empirical method involve a duality. Besides grasping the intelligibility immanent in data in a positive fashion, human intelligence also grasps a domination of the concrete by the abstract-and-systematic. However, though the duality is unfact.

one admits this duality as a fact, one still may ask whether it is ultimate, whether classical and statistical inquiries are isolated or related procedures, whether they lead to isolated or related results. An answer to these questions is sought in the present chapter, and it falls into three parts.

First, it will be advanced that classical and statistical investigations are complementary as types of knowing. In their heuristic anticipations, in their procedures, in their formulations, in their differences of abstractness, in their verification, and in their domains of data, each will be shown to complement and to be complemented by the other.

Secondly, besides the complementarity in knowing, there is a complementabily in the to-be-known. Whether one likes it or not, heuristic structures and empirical canons constitute an a priori. They settle in advance the general determinations, not merely of the activities of knowing, but also of the content to be known. Just as Aristotle's notions on science and method resulted in his cosmic hierarchy, just as the Galilean reduction of secondary to primary qualities necessitated a mechanist determinism, so too our simultaneous affirmation of both classical and statistical investigations involves a world view. That is that view?

involves a world view. What is that view? Thirdly, there is a clarification that results from contrast. Accordingly, after endeavoring to determine the world view, to which one commits oneself by accepting the heuristic structures and the canons of empirical method, there are set forth its differences from the world views of Aristotle, Galileo, Darvin, and contemporary indeterminists.

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Such than is the program of this chapter. Classical and statistical investigations are complementary as forms of mowing. They also are complementary investigation inverse they orthine involves a conditioned grizs series of schemes of recurrence, to which both classical and statistical laws are relevant. 

# Complementaries to in the Known

1.1, First, the heuristic anticipations of classical and of statistical procedures are complementary. For the systematic and the non-systematic are the contradictory alternatives of a dichotomy. Inquiry of the classical type is an anticipation of the systematic. Inquiry of the statistical type is an anticipation of the non-systematic. Now the relations between data must be either systematic or non-systematic. It follows that in any given case either the classical or the statistical acticipation must be correct.

Two corollaries follow.

The first is the openness of empirical method. The mare fact of inquiry is itself a presupposition, for it implies that there is something to be known by understanding the data. Still this presupposition is inevitable, for it makes marks the difference between the scientific and the non-scientific attitudes to experience. Moreover, this presupposition is minimal. For it does not determine a priori whether any selected range of data is to be reduced to system in a the classical fashion or, on the ks other hand, is to be accounted for by showing how the concrete diverges non-systematically from systematic expectations.

The second corollary is the relevance of empirical method. For empirical method is a matter of trial and error, and the only way to settle whether a given aggregate of observations are or are not reducible to system is to formulate both hypotheses, work out their implications, and test the implications against observed results.

# Complementer Procedures.

1.2 Next, classical and statistical pre investigations are complementary procedures. For they separate systematically and non-systematically related data, and the isolation of either type is a step towards the devermination of the other.

With such separation everyone is familiar when it is effected physically by experimentation. As has been seen, the aim of the experimenter is to isolate a definable conjunction of elements and to exhibit their operations as they occur when uninfluenced by extraneous factors.

Again, physical separation is not always possible, and then one attempts to do by thought what one cannot achieve by deed. In this fashion, as soon as a science has made some progress, it invokes its known laws in seeking the determination of the unknown. Thus, once Boyle's law is known, one assumes it in determining Charles' law; once both are known, one assumes both in determining Gay-Lussac's law. Similarly, in all departments, known laws are employed to guide experiment, to eliminate the consideration of what already has been explained, and to provide premises for the interpretation of observed results. Moreover, such separation, whether physical or

mental, is not confined to classical laws. All laws belong to a single complementary field. For this reason it has been

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possible to invoke the laws of probable errors and thereby to eliminate a non-systematic component in observations and measurements. In like manner, Mendel's statistical laws of macroscopic, genetic characters led to the postulation of microscopic entities named genes; to each gener was assigned, on the classical model, a single, determinate effect and manifestation; genes with incompatible effects were classified as dominant and recessive; and so statistical combinations of classically conceived genes became the explanation of non-systematic, macroscopic phenomena. The weader may be surprised that we lump together

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the laws of probable errors and the Mendelian laws of heredity. But from our viewpoint they belong together. In both cases a component in the data is brought under law. In both cases the discovery of the law grounds a mental separation of the component, subject to known law, from other components still to be determined. In both cases this mental separation opens the way to the determination of further laws. In both cases, finally, it is the discovery of a statistical law that grounds the mental separation and that can lead to the discovery no less of classical than of statistical laws.

This complementarity of classical and statistical procedures has an important corollary. For the experimental, physical exclusion of extraneous factors is not always possible. When it is not, there exists the alternative of discovering the law of the extraneous factor and then allowing for its influence in interpreting one's result. Now the corollary, to which we would draw attention, is that statistical laws can be employed in this fashion to the determination of classical laws. For knowledge of statistical laws enables one to separate mentally the non-systematic component in the data and so it leaves one free to investigate the remaining systematic component.

It will be asked, then, whether the statistical investigations of Quantum Mechanics may be expected to prepare the way for a later resurgence of classical thought in the field of sub-atomic physics.

This question is, I think, ambiguous. One may mean a return to the former type of classical thought with its imaginable models, its belief in the universal possibility of imaginative synthesis, its affirmation of a mechanist determinism, and its concept of explanation as the reduction of secondary to primary qualities. On the other hand, it is possible to speak of "classical" thought in a transposed and analogous sense. In that case, one would grant to imagination a notable heuristic value, for images supply the materials for m insights; but, at the same time, one would deny to unverified and unveriable images any representative value; classical laws would be conceived as abstract, must the abstraction would be conceived as enriching, and so full f knowledge of classical laws would not preclude the existence of statistical residues.

Once this distinction is drawn, our answer to the foregoing question becomes obvious. Wexaannes In the light of the canons of complete explanation, of parsimony, and of statistical residues, we cannot expect any return to the older type of classical thought. Again, in the same light, we must expect Quantum Mechanics, if interpreted statistically, to open the way to a new development of "classical" thought in a transposed and analogous sense. Indeed, Pauli's exclusion principle provides a premise for the determination of the states of electrons in atoms; and while changes of these states seem to occur statistically,

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still the series of states is as regular and systematic as the periodic table of chemical elements (see Lindsay and Margenau, pp.488f.) In like manner, one might note classical tendencies in the discovery of new sub-atomic entities over and above the more familiar electrons, protons, and neutrons.

are complementary.

For classical laws hold under the provise, other things being equal. Still, what are the other things? In what does their equality consist? As has been argued at some length (Chapter III, §6.), events occur on the fulfilment of a diverging series of conditions, and the totality of patterns of such diverging series form a non-systematic aggregate. Now classical laws are verified in events, and so it follows that they are verified as often as a relevant mattern of diverging iditions is fulfilled

Complementary Formulations

1.3 A Thirdly, classical and statistical formulations are complementary. For classical formulations regard conjugates, which are verified only in events. And statistical formulations regard events, which are defined only by conjugates.

The dependence of classical upon statistical formulation comes to light, when one probes into the meaning of the classical proviso, other things being equal. That are the other things? In what does their equality consist? These questions cannot be given an answer that is both detailed and systematic. For the proviso, which limits classical laws, is effectively any relevant pattern of a diverging series of conditions. Such series vary with circumstances, and the aggregate of patterns of such series is both enormous and non-systematic. In other words, classical laws tell what would happen in if conditions were fulfilled; statistical laws tell how often conditions are fulfilled; and so the phrase, other things being equal, amounts to a vague reference to the statistical residues, which are the province of the complementary statistical laws.

The inverse dependence of statistical upon classical formulations comes to light, when one asks which statistical investigations possess scientific significance. Thus, anyone would acknowledge a difference in such significance between determining the frequency of red hair in trombone players and, on the other hand, measuring the intensity of line spectra. In either case one arrives at a number that may be regarded as an actual frequency, but it is not apparent that in both cases one has an equal chance in contributing to the advance of science. For the advance of science is secured by operating in whe light of present knowledge and towards the solution of well-formulated problems. As soon as any department of science hes passed beyond its initial stages, it begins to desert the expressions of ordinary language and to invent technical terms of its own. Such technical terms have their origin in the correlations that have been found significant; they are or, in some fashion, they depend upon what we have named pure conjugates. Accordingly, inasmuch as the statistical investigator proceeds in the light of acquired knowledge and towards the solution of well formulated problems, he will be led to define events by appealing, directly or indirectly, to the pure conjugates that

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However, the reader may ask whether this view can be regarded as definitive. It is true enough that the scientific classifications and definitions of the present are dependent on the discovery and formulation of classical laws. But may one not expect that a fuller development of statistical inquiry will result in the implicit definition of technical terms by statistical and not classical laws?

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his question of irrestively. I cannot see my way to agreeing with hem. My reason runs as follows. Statistical laws refer to events. Events stand to defining conjuctes, whether existent and experiential or pure, as the answer, "Yes," to a question for reflection stands to the descriptive or explanatory answer to a question for intelligence. For the event is simply the happening, the occurring, that stands in need of definition and can obtain it only by shifting from the question, "...bether?" to the different type of question, "...bether?" of this showing, then, as long as "Yes" obtains its meaning precise meaning by reverting to a prior question,

Jhile there seem to be those that woold answer this question effirmatively, I cannot see my way to agreeing with them. My reason runs as follows. The answer, "Yes, to a question for reflection obtains a determinate meaning only by reverting from the "Yes" to the question and to its origin in the another descriptive or explanatory answer to a question for x intelligence. Now the event, the happening, the occurring corresponds to the bare "Yes." To say what happens, what occurs, one must raise a question that cannot be answered by a "Yes" or a "No." One must appeal either that to the experiential conjugates of description or to the explanatory pure conjugates of explanation. On this showing, then, one cannot expect events to generate their own definitions any more than one can expect "Yes" or "No" to settle what is affirmed or denied. Finally, if events cannot generate their own definitions, then frequencies of events cannot do so; for there seems no reason to expect that different types of events must have different numerical frequencies or, indeed, that the numerical frequencies could serve to specify the kinds of events to which one wishes to refer.

There is, then, a complementarity of classical and statistical formulations. For if statistical formulations are to be significant contributions to the advance of science, they will appeal to the experiential and pure conjugates of classical elessical classifications and definitions. Inversely, the conjugates of classical formulations are verifiable only in statistically occurring events and their immanence in statistical residues is revealed by the provise, "other things being equal."

It may not be out of place to conclude this sub-section by clarifying a slight puzzle. It is true enough that statistical laws also are immanent in statistical residues, and so hold under the general proviso, "other things being equal." If "P follows Q" has the probability, p/q, still there are conditions for the occurrence of the occasion, Q, and it is only when those conditions are fulfilled that the probability, p/q, is verifiable. The frequency of such fulfilment might be indicated by saying that "Q follows R" has the probability, q/r, so that one statistical law would be dependent on another.

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Still this inter-dependence of statistical laws, while true dates the significant contention that the dependence of classical upon statistical formulations is revealed by the proviso, "Other things being equal."

Complementer Modes & Abtration. 4 Fourthly, there is a complementarity in modes of abstraction.

Classical heuristic procedure rests on the assumption that to some extent the relations between data are systematic, and it devotes its efforts to determine just what those re systematic relations are.

Statistical heuristic procedure rests on an assumption of managetmaling non-systematic relations and it aims at determining an ideal frequency from which actual frequencies may diverge but only non-systematically.

In both cases the result obtained is abstract. For the classical law represents the systematic and prescinds from the non-systematic. On the other hand, the statistical law represents, not the actual frequency of actual events, but the ideal frequency from which actual fre uencies diverge.

Now while both types of law are abstract, still their modes of absoraction differ. The classical law is concerned simply with the systematic; it disregards the non-systematic. The statistical law, on the contrary, assumes the non-systematic as a premise. By itself, of course, such a premise could yield no conclusions such as the abstract, ideal, universal frequencies named probabilities. What concerns the statistical inquirer is, then, neither the purely systematic, nor the purely non-systematic, but the systematic as setting ideal limits from which the nonsystematic cannot diverge systematically.

Clearly, these two modes of abstraction are complementary. In its first movement, in diry aims beadetermining the systematic component in data; in its second movement, inquiry turns to the more concrete task of determining how the manner in which the systematic component in data moderates the non-systematic. The complete view results only from the combination of the two movements, and so the two are complementary.

There is another aspect to this complementarity. The systematic relations, which with which classical inquiry is concerned, mainly are the relations of things, not to our senses, but to one another. In so far as the relations of things to one another are considered in the abstract and so as independent of their relations to our senses, there arises a principle of equivalence for all senses since all equally are abstracted from. On the other hand, statistical laws deal, not simply with occasions and events, but with observable occasions and observable events. They are not, in principle, independent of the relations of things to our senses, and so they cannot be subjected to a full principle of equivalence. Wassed There follows the already mentioned formal opposition between Quantum Mechanics, isterpreted statistically, and General Relativity; the two theories may deal with the same things, but they deal with them from radically different viewpoints: they are complementary in so far as General Relativity is concerned with things as independent of their relations to our senses while Quantum Mechanics views team things in a manner that includes those relations. [See Chapter III, §6.64].

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# Complementanty in Verylication

1.5 Fifthly, classical and statistical laws are complementary in their verification. This may be stated roughly by saying that classical laws determine what would happen if conditions were fulfilled, while statistical laws determine how often one may expect conditions to be fulfilled. However, a fuller account of this complementarity may be given by showing how the determination of entry elther classical or statistical laws leaves room for the determination of the other.

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Thus, if one were to suppose exact and complete knowledge of all classical laws, one would not preclude the possibility of the verification of statistical laws. Let us say blass a set of classical laws, say P, would be exact and complete, if there were no possibility of replacing them by some different set, say Q. ATHON, there would be no possibility of replacing P by M Q, if there were no systematic divergence between the data and the set of laws, P; for the sets, P and Q, differ as laws and so differ systematically; and so the verification of the set, Q, in place of the set, P, supposes a systematic divergence between the set, P, and the data. Finally, though there is no systematic divergence between the set, P, and the data, there can be a non-systematic divergence that would provide the field for the investigation and verification of statistical laws. Again, as has been seen (Chapter III, §6. ),

can/ exact and complete knowledge of classical laws not merely/leaves room for possible statistical investigation but also must do so. For such exact and complete knowledge would embrace all the systematic relations between determinate data; none the less, such knowledge would be abstract and so in need of further determinations to be applied to concrete instances; it follows that the further determinations cannot be systematically related to one another, and so that there must be a field for statistical laws.

Finally, statistical investigations in their turn have nottendency to totalitarian asparations. For besides statictical predictions, there exist the fully accurate predictions that are exemplified by astronomy and that rest on the existence of sekarsof schemes of recurrence. Suchaschemes Moreover. the invelligent manner of making these predictions is to analyse the schemes into their component classical laws. Comernicus corrected Ptolemy's imaginative scheme; Kepler corrected the circles of Copernicus; but it was Newton that worked out the underlying laws and Laplace that revealed the periodicity of the planetary system. From that discovery of laws the great movement of thought, named modern science, received its most powerful confirmation. It did so because it ended, at least for two centuries, the more common human tendency to speak, not of precise laws, but of the common run of events or the ordinary course of Nature. At the present moment, the profound significance of statistical laws is coming to light. But if this new movement is not to degenerate into the old talk about what commonly happens, it must retain its contact with the empirically established precision of classical formulations. For statistical laws are of no greater scientific significance what the definitions of the events whose frequencies they determine; unless those definitions are determined scientifically, statistical thought lapses into pre-scientific insignificance.

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# Complementerity in Data Caplemid.

1.6 A Sixthly, classical and statistical laws are complementary in their domains of data. By this is meant, not that some data are explained by classical laws and other data by statistical laws, but rather that certain aspects of all data receive the classical type of explanation while other aspects of the same data are explained along statistical lines.

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As has been seen (Chapter II, §2.3), the classical heuristic assumption is that similars are similarly understood. Consequently, preliminary classifications are based on similarity to sense. However, the scientist is interested in the relations of things, not to our senses, but to one another. Accordingly, the preliminary classifications are superseded by the emergence and development of technical terms that are derived, not from sensible similarity, but from similarities of constant and regularly varying proportion; and in the limit there are reached what we have named pure conjugates, that is, terms implicitly defined by the empirically established correlations in which they occur.

Still to account for data as similar is not to account for data in all their aspects. Each datum is just this instance of the given. It emerges within a continuous manifold. It is **m**txx in a particular place and at a particular time. It occurs rarely or frequently. Now these aspects of all data are disregarded in explanations of the classical type. The law of the lever tells us nothing about the frequency of levers, about the places where they are to be found, **thertimes** about the times at which they function. Hence, explanations of the classical type have to be complemented by explanations of a further, different type.

Nor is it difficult to see, at least in some general fashion, that statistical laws can provide the complementary explanation. For the general form of the statistical law is that on <u>p</u> occurrences of the occasion, P, there tend to be <u>g</u> occurrences of the event, Q. Now the occasion, P, is itself an event or a combination of events. In either case it will possess its probability. In like manner, the occasions on which P is probable, will have their probability, and so there arises an indefinite regress of probabilities from events of the type, Q. More generally, for events of any type, X, there are corresponding indefinite regresses of probabilities.

Now, it is not immediately apparent that such regresses can be combined into a single view. But it suffices for present purposes to remark that, were such a combination possible, one would be on the wys way to attaining a statistical explanation of data in their numbers and in their spatio-temporal distribution. To invoke only the simplest considerations, low probabilities are offset by large numbers of occasions, so that what is probable only once inxa on a million oacasions, is to be exjected a million times on a million million occasions. In like manner, the rarity of occasions is offset by long intervals of time, so that if occasions arise only once in a million years, still they arise a thousand times in a thousand million years. At once there emerges the explanatory significance of statistical laws. Why are there in the world of our experience such vast numbers and such enormous intervals of time? Because probabilities are low, numbers have to be large; because occasions are rare, time intervals have to be long.

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By itself, this is a very modest conclusion. Still, though the achievement is quite negligible, the potentialities are extremely significant. Statistical laws possess a capacity to generate explanation. Their heuristic assumption is simply that the non-systematic cannot diverge systematically from the systematic. But this incapacity for systematic divergence, is equivalent when combined with large numbers and long intervals of time, is equivalent to a positive tendency, to an intelligible order, to an effective thrust, that is no less explained than the rigorous conclusions based on classical laws. In other words, probability is one thing, and chance is another. Probability is an ideal norm that, for all its ideality, is concretely successful in the long run. Chance is merely the non-systematic divergence of actual frequencies from the ideal frequencies named probabilities. Chance explains nothing. It pertains irretrievably to the x morely empirical residue, to the aspects of data from which intelligence always abstracts. But probability is an isolligibility rescued from the verely empirical residue. By the round about davice by Whiteh inviting inter 1 sence is an intelligibility; it is, as it were, rescued from the merely empirical residue by the round-about device in which inquiring intelligence sets up the heuristic anticipations of the statistical type of investigation.

momen. 1.7 We have been considering the complementarity of classical and statistical investigations as forms of knowing. We have found such complementarity to exist at each of the stages or components of the process of incuiry. There is the classical huristic anticipation of the systematic; there is the complementary statistical heuristic anticipation of the nonsystematic. Next, to determine either a classical or a statistical law is to prepare the way for the determination of further laws of either type; for both classical and statistical laws pertain to a single complementary field, and to know either is to effect a mental separation between types of data that have been accounted for and types that still remain to be explained. Thirdly, there is a complementarity of formulations: the experiential and pure conjugates of classical laws can be de verified only in events; the events occur only if other things are equal; and the equality of other things amounts to an unconscious ackno. ledgement of the non-systematic aggregate of patterns of diverging series of conditions. Inversely, as conjugates are verified only in events, so events are defined only by conjugates, and statistical laws of events can possess scientific significance only in the measure that they employ definitions guerated by classical procedures. Fourthly, there is a complatementarity in modes of abstraction: classical laws regard the systematic in abstraction from the non-systematic, the relations of things to one another in abstraction from their relations to our senses; but statistical laws consider the systematic as setting bounds to the non-systematic and they are confined to the observable events that include a relation to out senses. Fifthly, the two types of law are complementary in their verification: exact and complete knowledge of classical laws cannot successfully invade the field of statistical laws; and statistical investigations are confronted with regular recurrences that admit explanations of the classical type. Finally, there is complementarity in the aspects of data explained by the different types of laws; data as similar are explained on classical lines; but their numbers and their distributions become intelligible only by some synthesis of statistical considerations.

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# Complementanty in the Known 2.0 Just as

Just as the first part of this chapter was devoted to exhibiting the complementarity of classical and of statistical investigations from the viewpoint of knowing, so now the second part is to be directed to the decerminations of the corresponding complementarity from the viewpoint of what is to be known. For knowing and known, if they are not an identity, at least stand in some correspondence and, as the known is reached only through knowing, structural features of the one are bound to be reflected in the other. Aristotle's world-view stemmed from his distinction between the necessary laws of the heavenly bodies and the contingent laws of things on this earth. Mechanist determinism had its scientific basis in the Galilean concept of sc explanation as the reduction of secondary to primary qualities. In similar fashion some parallel implication cannot be avoided by any fully conscious methodology and so, if we are not to play the ostrich, we must face the question, what worldview is involved by our affirmation of both classical and statistical laws.

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General Charituctic Atte View Cortain general characteristics of our position 2,1 may be indicated immediately.

In the first place, it will be concerned with the intelligibility immanent in the universe of our experience. For it will be a conclusion from the structure of empirical method and, by the canon of relevance, empirical method is confined to determining such immanent intellicibility. Hence, we shall have nothing to say in this chapter about the end or purpose of this universe, about the materials from which it was fashioned, about the principal or instrumental agents responsible for it. Our efforts will be limited to determining the immanent design or order characteristic of a universe in which both classical and statistical laws obtain.

In the second place, our account of this design or order will be generic. A specific account would have to draw upon the content of the empirical sciences. It would have to appeal, not to classical and statistical laws in general, but to the precise laws that can be empirically established. Our account, on the other hand, will rest not on the results of scientific investigations but simply and solely upon the dynamic structure of inquiring intelligence. Accordingly, if in the course of the exposition any particular scientific conclusions are invoked, their function will be not determinative but merely illustrative. Just as mechanist determinism has been a world-view that is independent of the precise content of classical laws, so too our objective is a similarly generic structure that is compatible not only with present classical and statistical laws but also with their future revisions.

In the third place, our account of the design or order of this universe will be relatively invariant. The concent of the natural sciences is a variable. There has been the schence of the Renaissance. There has been the science of the Enlightenment. There is the science of today. There will be the successive stages of scientific development in the future. But knitting together these diverse manifestations of scientific thought, generating each in turn only to bring forth the revision and transformation of each, there is the underlying invariant that loosely may be named scientific method and more precisely,

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I think, would be designated as the dynamic structure of inquiring intelligence. For, as has been seen, it is the desire to understand that results both in the heuristic structure of classical procedure and in the complementary structure of statistical investigation; and it is the nature of insight that accounts for the six canons of selection, operations, relevance, parsimony, complete explanation, and statistical residues, in accord with which the heurxistic structures generate the series of scientific theories and systems. Now our premst premise is to be, not the variable contents of the sciences, but the invariant forms coverning scientific investigation. It follows that the design of the universe, to which we shall conclude, will enjoy the invariance of the premise, for which we shall invoke.

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Still, I have said that our account will be only relatively invariant, and the reason for this restriction is plain enough. For our appeal will be, not to the structure of the human mind itself, but only to our account of that structure. Just as the natural sciences are subject to revision, so too one may expect our account of inquiring intelligence to be subjected to rearrangements, modifications, and improvements. In the measure that such changes will affect the premises of the present argument, in the same measure they will also affect the conclusions. Accordingly, the world-view to be presented will be invariant, inasmuch as it will be independent of changes in the content of the natural sciences; but it will be only relatively invariant, for it cannot be independent of res revisions of our analysis of empirical method.

In the fourth place, our account of a world-view within the limits of empirical science will not be complete in this chapter. In treating the canon of parsimony, we postponed the question of the validity of the notion of the thing. In a later chapter, that question will have to be met, and then a further complement to the present account will be added.

In the fifth place, our account will not claim to be deductive. Perhaps one might argue in strictly deductive fashion from the complementary structure of the knowing to the corresponding complementarity of the known. But, if that procedure is possible, it also requires an elaboration that for present purposes would be excessive. Accordingly, our appeal will be to insight. We shall begin from the problem of showing how both classical and statistical laws can coalesce into a single, unified intelligibility commensurate with the universe of our experience. Against this problem we shall set our clue, namely, the scheme of recurrence. On the one hand, the world of B our experience is full of continuities, oscillations, rhythms, routines, alternations, circulations, regularities. On the other hand, the scheme of recurrence not only squares with this broad fact but also is related intimately both to classical and to statistical laws. For the notion of the scheme emerges in the very formulation of the canons of empirical method. Abstractly, the scheme itself is a combination of classical laws. Concretely, schemes smargs begin, continue, and cease to function in accord with statistical probabilities. Such is our clue, our incipient insight. To develop it we shall consider 1) the notion of a conditioned series of schemes of recurrence, 2) the probability of a single scheme, 3) the emergent probability of a series of schemes, and 4) the consequent characteristics of a world order.

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Schemes Recursive and 2.2 The notion of the scheme of recurrence, emerged when it was noted that the diverging series of positive conditions for an event might coil around in a circle. In that case, a series of events, A, B, C,... would be so related that the fulfilment of the conditions for each would be the occurrence of the others. Schematically, then, the scheme might be represented by the series of conditionals, If A occurs, B will occur; if B occurs, Cik will occur; if C occurs,... A will recur. Such a circular arrangement may involve any number of terms, the possibility of alternative routes, and in general any degree of complexity. Moreover

Two instances of greater complexity may be noted. On the one hand, a scheme might consist of a set of almost complete circular arrangements, of which none could function alone yet all would function if conjoined in an inter-dependent combination. On the other hand, schemes might be complemented by defensive circles, so that if some event, F, tended to upset a scheme, there would be some such sequence of conditions as, If F occurs, then G occurs; if G occurs, then H occurs; if H occurs, then F is eliminated.

In illustration of schemes of recurrence the reader may think of the planetary system, of the circulation of water over the surface of the earth, of the nitrogen cycle familiar to biologists, of the routines of animal life, of the repetitive rhythms of production and exchange. In illustration of schemes with defensive circles, one may advert to generalized equilibria. Just as a chain reaction is a cumulative series of changes terminating in an explosive difference, so a generalized equilibrium is such a combination of defensive circles that any change, within a limited range, is offset by opposite changes that tend to restore the initial situation. Thus, health in a plant or animal is a generalized equilibrium; again, the balance of various forms of plant and animal life within an environment is a generalized equilibrium; again, economic process was conceived by the older economists as a generalized equilibrium.

However, we are concerned, not with single schemes, but with a conditioned series of schemes. Let us say that the schemes, P, Q, R,... form a conditioned series, if all prior members of the series must be functioning actually for any later member to become a concrete possibility. Then, the scheme, P, can function though neither Q nor R exist; the scheme, Q, can but may not be functioning, if the scheme

owin no function mless the schemer, P. is already a prative: the sector, R, could not function unless both P and & were functioning an innotion, thou h R does not exist; but & connet function unless is already functioning and B ansot Function unless

can function, though R does not yet exist; but Q cannot function unless P is already functioning; and R cannot function unless Q is already functioning.

Thus, by way of a simple illustration, one may advert to the dietary schemes of animals. All carnivorous animals cannot live off other carnivorous animals. Hence, a carnivorous, dietary scheme supposes another herbivorous, dietary scheme but, inversely, there could be herizbivorous animals without any carnivorous animals. Again, plants cannot in genral general live off animals; the scheme of their nourishment involves chemical processes; and that scheme can function apart from the existence of any animals. Finally, chemical cycles are not

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independent of physical laws yet, inversely, the laws of physics can be combined into schemes of recurrence that are independent of chemical processes.

Such in briefest outline is the notion of the conditioned series of schemes of recurrence. Let us seek a slight increase in precision by drawing a threefold distinction between 1) the possible seriation, 2) the probable seriation, and 3) the actual seriation.

The actual seriation is unique. It consists of the schemes that actually were, are, or will be functioning in our universe along with precise specifications of their places, their durations, and their relations to one another.

The probable situation seriation differs from the actual. For the actual diverges non-systematically from probability expectations. The actual is the factual, but the probable is ideal. Hence, while the actual seriation has the uniqueness of the the matter of fact, the probable seriation pathbits not only the chernetives thet have been conficted internatives that would have been conficted has to exhibit the constantive remifications of probable alternatives, a line of meximum recommitty, and a series of times of lesser probability

hes to exhibit the cumulative ramifications of probable alternatives. Accordingly the probable seriation is not a single series but a manifold of series. At each stage of world process there are a set of probable next stages, of which some are more probable than others. The actual seriation includes only the stages that occur. The probable seriation includes all that would occur without systematic divergence from the probabilities.

The possible seriation is still more remote from actuality. It includes all the schemes of recurrence that could be devised from the classical laws of our universe. It orders them in a conditioned series that ramifies not only along the lines of probable alternatives but also along lines of mere possibility or negligible probability. It is equally relevant to our universe and to any other universe subject to the same classical laws, no matter what its initial numbers, diversities, and distribution of elements.

Of the three seriations, then, the possible exhibits the greatest complexity and veriety. It de ends solely on a consideration of classical laws. It suffers from the indeterminacy of the abstract, and so exhibits the process of any universe with sinilar laws similar to ours. The probable seriation depends on statistical as well as classical laws and, indeed, on the statistical laws that arise from the initial or basic situation of our world. Still, if it is not as abstract as the possible seriation, none the less it is ideal. For each moment of world history, it assigns a most probable future course. But it also assigns a series of less probable courses, and it has to acknowledge that any of these may prove to be the fact. Finally, the actual sri seriation is unique, but it purchases its uniqueness by going beyond the field of all laws, classical and statistical, and entering the field of observation, in which alone non-systematic divergences from probability are determinate.

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# The Probability ASchemes.

2.3 Contribute of the notion of a conditioned series of schemes of recurrence supposes that one can attribute a probability to the emergence and to the survival of a scheme of recurrence. However, our account of probability has been in terms of the frequency, sfrequents not of schemes, but of events. Have schemes any probability? If they have, is there a distinct probability for their emergence and another for their survival? Such questions must be met.

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Consider a set of events of the types, A, B, C,... and a world situation in which they possess respectively the probabilities, p, q, r,... Then by a general rule of probability theory, the probability of the occurrence of all the **xents** events in the set will be the product, <u>per...</u>, of their respective probabilities.

Now let us add a further assumption. Let us suppose that the set of events, A, B, C,... satisfy a conditioned scheme of recurrence, say K, in a world situation in which the scheme, K, is not functioning but, in virtue of the fulfilment of prior conditions, could begin to function. Then, if A were to occur, B would occur. If B were to occur, C would occur. If C were to occur,... A would occur. In brief, if any of the events in the set were to occur then, other things being equal, the rest of the events in the set would follow.

In this case we may suppose that the probabilities of the single events are respectively the same as before, but we cannot suppose that the probability of the combination of all events in the set is the same as before. As is easily to be seen, the concrete possibility of a scheme beginning to function shifts the probability of the combination from the product, <u>pqr</u>..., to the sum,  $p + q + r + \cdots$ . For, in virtue of the scheme, it now is true that A and B and C and... will occur, if either A or B or C or... occur; and by a general rule of probability theory, the probability of a set of alternatives is equal to the sum of the probabilities of the alternatives. Now a sum of a set of/fractions, p, q, r,... is

Now a sum of a set of/fractions, p, q, r,... is always greater than the product of the same fractions. But a probability is a profer fraction. It follows that, when the prior conditions for the functioning of a scheme of recurrence are satisfied, then the probability of the combination of events, constitutive of the scheme, leap from a product of fractions to semething lass a sum of fractions.

There exists, then, a probability of emergence for a scheme of recurrence. That probability consists in the sum of the respective probabilities of all the events included in the scheme, and it arises as soon as the prior conditions for the functioning of the scheme are satisfied.

there is also a probability for the survival of chemes of recurrence. For the scheme involves a combination of classical laws which bold concretely under the roviso, other things boung equal. Now that provise, as has been seen, refers to the non-systematic and is subject to statistical valuation

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There also exists a probability for the survival of schemes that have begun to function. For, of itself, a scheme tends to assure its own perpetuity. The positive conditions for the occurrence of its component events reside in the occurrence of those events. Even negative conditions, within limited ranges, can be provided forth by the development of defensive curcles. None the less, the perpetuity of a scheme is not necessary. Just as classical laws are subject to the provise, other things being equal, so also are the schemes constituted by combinations of classical laws; and whether or not other things will continue to be equal, is a question that admits an answer only in terms of statistical laws. Accordingly, the probability of the survival of a scheme of recurrence is the probability of the non-occurrence of any of the events that would disrupt the scheme.

### Emergent Probability

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There have been formulated the notion of a 2.4 conditioned series of schemes of recurrence and, as well, the general sense in which one can speak of the probability of the emergence and the survival of schemes: single schemes. From these considerations there now comes to light the notion of an emergent probability. For the actual functioning of earlier schemes in the series fulfils the conditions for the possibility of the functioning of later schemes. As such conditions are fulfilled, the probability of the combination of the component events in a scheme jumps from a sam product of a set of proper fractions to the sum of those proper fractions. But, what is probable, sooner or later occurs. When it occurs, a probability of emergence is replaced by a probability of survival; and as long as the scheme survives, it is in its turn fulfilling conditions for the possibility of still later schemes in the series.

Such is the general notion of emergent probability. It results from the combination of the conditioned series of schemes with their respective probabilities of emergence and survival. While by itself it is extremely jejune, it possesses rather remarkable potentialities of explanation. These must now be indicated in outline, and so we attempt brief considerations of the significance for emergent probability of spatial distribution, absolute numbers, long intervals of time, selection, stability, and development.

The notion of a conditioned series of schemes involves spatial concentrations. For each later set of schemes becomes possible in the places where earlier schemes are already functioning. Accordingly, the most elementary schemes, which are earliest in the series, can occur anywhere in the initial distribution of materials. But the second batch can occur only where the first have in fact occurred, the third can occur only where the second have in fact occurred, and so on. Moreover, since the realization of the schemes is in accord with the probabilities, which may be low, one cannot expect all possibilities to be actuated. Hence, elementary schemes will not be as frequent as they could be, to narrow the possible basis for schemes at the second remove. These will not be as frequent as they could be, to narrow again the possible basis for schemes at the third remove, and so forth. It follows that, however widespread the realization of constrictions of the volumes of space in which later schemes can be found. Similarly, it follows that the

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points, so to speak, of greatest and least constriction occur where the probabilities of emergence of the next set of schemes are respectively the lowest and the highest. Finally, it follows that, since the latest schemes in the series have the greatest number of conditions to be fulfilled, their occurrence will be limited to a relatively small number of places.

Secondly, there is the significance of absolute numbers. For large numbers offset low probabilities. That occurs once on a million occasions, is to be expected a million times on a million million occasions. Now the minimum probability pertains to the latest schemes in the series, for their emergence supposes the emergence of all earlier schemes. It follows that the lower the probability of the last schemes of the conditioned series, the greater must be the initial absolute numbers in which elementary schemes can be realized. In brief, the size of a universe is propartionate to the probability of its ultimate schemes of recurrence.

Thirdly, there is the significance of long intervals of time. No matter how great the universe and how widespread the functioning of elementary schemes, there is an increasing concentration of the spatial volumes in which later schemes can be realized. Sconer or later, the initial benefit of large numbers is lost by the successive narrowing of the basis for further developments. But at this point long intervals of time become significant. Just as a million million simultaneous possibilities yield a million probable realizations, whose probabilities is one in a million, so also a million million successive possibilities yield a million probable realizations under the same expectation.

Fourthly, there is a selective significance attached to the distinction between probabilities of emergence and probabilities of survival. If both are low, the occurrence of the scheme will be both rare and fleeting. If both are high, the occurrence will be both common and enduring. If the probability of emergence is low and that of survival is high, the scheme is to be expected to be rare but enduring. Finally, in the opposite case, the expectation is that the scheme will be common but fleeting. Fifthly, this selectivity has its significance

for stability. The functioning of later schemes depends upon the functioning of earlier schemes, so that if the earlier collapse, then the later will collapse as well. It follows that the line of maximum stability would be of common and enduring schemes while the line of minimum stability would be of rare and fleeting schemes.

to be considered. For schemes with high probabilities of emergence and of survival are not to be a road-block on the way to development. They provide a highly secure basis for later schemes, but they are likely to prevent the emergence of any later schemes. Because their probability of emergence is high, they tend to because a large proportion of possibilities of development.

Because their probability of emergence is nigh, they tend to because their probability of survival is high they cling tenaciously to the optortunities they have seized. A universe that consisted mainly of the inert gases would be highly stable, but it would purchase stability by excluding development. Accordingly, the line that combines both stability and developmental potentialities would make use of a floating popth population of earlier schemes that were both common and floating; because they were common, the collapse of some would be easily replaced by the emergence of others; because they were flecting, their rapid disaprearance

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Sixthly, no less than stability, the possibility of development must be considered. Unfortunately, these two can conflict. Schemes with high probabilities of survival tend to im rison materials in their own routines. They provide a highly stable basis for later schemes, but they also tend to prevent later schemes from emerging. A solution to this problem would be for the/conditioning schemes to be a floating papulation of Connon but floating schemes to have a high probability of emergence but a low probability of servival. They would form a floating population, on which later schemes could successively depend. Because their probability of survival was low, they would readily surrender materials to give later schemes the characture opportunity to emerge. Because their probability of emergence was high, they would readily be availabile to fulfil the conditions for the functioning of later schemes.

Needless to say, the foregoing considerations are extremely rudimentary. They are limited to the emergent probability of any conditioned series of schemes of recurrence. They make no effort towards developing that notion in the direction of its application to the conditions of the emergence and survival of modes of living. However, while absolutely such a fuller exposition would be desirable, still it has no place in a merely generic account of world order. For the premise of a generic account is, not the content of the natural sciences, but the possibility and validity of their assumptions and method.

Horeover, to look for a deteiled expesition nould be to miss the point of what he are son trying to say. The have Turnulated a notion of energent brobability and briefly considered aspects of its significance

The point we are endeavoring to make, within the limits of our narrow premise, is that the notion of emergent probability is explanatory. Intelligent induiry aims at insight. But classical laws alone offer no insight into numbers, distributions, concentrations, time intervals, selectivity, uncertain stability, or development. On the contrary, they abstract from the instance, the place, the time, and the condrete conditions of actual functioning. Again, statistical laws, as/mere aggregate, affirm in various cases the ideal frequency of the occurrence of events. They make no pretence to explaining why there are so many kinds of events or why each kind has the frequency attributed to it. To reach explanation on this level it is necessary to effect the concrete synthesis of classical laws into a conditioned series of schemes of recurrence, to establish that such schemes, as combinations of events, acquire first a probability of emergence and then a probability of survival through the realization of the conditioned series, and finally to grasp that, if such a series of schemes is being realized in accord with probabilities, then there is available a general principle that promises aznswers to questions about the reason for numbers and distributions, concentrations and time intervals, selectivity and uncertain stability, development and breek-downs. To work out the answers pertains to the natural sciences. To grasp that emergent probability is an explanatory idea, is to know what was meant when xexsaid our objective was characterized as a generac, relatively invariant, and incomplete account of the immanent intelligibility, the order, the design of the universe of our experience.

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# Consequences 1/ Emergent Probability.

2.5 There remains the task of working out the generic properties of a world process in which the order or design is constituted by emergent probability. This we shall attempt in two main steps. First, we shall summarize the essentials of the notion of emergent probability. Secondly, we shall enumerate the consequences of that notion to be verified in world process.

The essentials of the notion of emergent probability may be indicated in the following series of assertions.

An event is what is to be known by answering "Yes" 1. to such questions as, Did it happen? Is it occurring? Will it occur?

World process is a spatio-temporal manifold of 2. events. In other words, there are many events and each has its place and time.

Events are of kinds. Not every event is a new 3. species, else there could be neither classical nor statistical laws. Events are recurrent. There are many events of 4. each kind, and all are not at the same time.

5. There are regularly recurrent events. This regularity is understood, inasmuch as combinations of classical laws yield schemes of recurrence. Schemes are circular relationships between events of kinds, such that if the events occur once in virtue of the circular relationships then, other things being equal, they keep on recurring indefinitely.

Schemes can be arranged in a conditioned series, 6. such that the earlier can function without the emergence of the later, but the later cannot emerge or function unless the earlier already are functioning.

Combinations of events possess a probability, and 7. that probability jumps, first when a scheme becomes concretely possible in virtue of the fulfilment of its prior conditions, and secondly when the scheme begins actually to function.

8. The actual frequencies of events of each kind in each place and at each time doss not diverge systematically from their probabilities. However, actual frequencies may diverge non-systematically from probabilities, and that non-systematic divergence is chance. Accordingly, probability and chance are distinct and are not to be confused.

Emergent probability is the successive realization 9. in accord with probability successive schedules of probability of a conditioned series of schemes of recurrence.

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in the possibilities it contains and the probabilities it contains are the schemes that could emerge in that situation; and these possibilities mainly rest on a the actual functioning of earlier,

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The consequent properties of a world process, in which the design is emergent probability, run as follows.

1. There is a succession of world situations. Each is characterized 1) by the schemes of recurrence actually functioning, 2) by the further schemes that now have become concretely possible, and 3) by the current schedule of probabilities of survival for existing schemes and of probabilities of emergence for concretely possible schemes.

2. world process is open. It is a succession of probable realizations of possibilities. Hence, Mense it does not follow the rigid rule wide down by addrenations to run along the iron rails laid down by determinists nor, on the other hand, is it a non-intelligible morass of merely chance events.

3. Ford process is increasingly systematic. For it is the successive realization of a conditioned series of schemes of recurrence, and the further the series of schemes is realized, the greater the systematization to which events are subjected.

4. The increasingly systematic character of world process is assured. No matter how slight the probability of the realization of the most developed and most conditioned schemes, the emergence of those schemes can be assured by sufficiently increasing absolute numbers and sufficiently prolonging intervals of time. For actual frequencies do not diverge systematically from probabilities; but the greater the numbers and the longer the time intervals, the clearer the need for a systematic intervention to prevent the probable from occurring.

5. The significance of the initial or basic world situation is limited to the possibilities it contains khe and to the probabilaties it assigns its possibilities. By the initial world situation is meant the situation that is first in time; by the basic world situation is meant the partial prolongation through time of initial conditions, such as arises, for instance, in certain contemporary hypotheses of continuous creation.

In either case, what is significant resides in possibilities and their probabilities, for in all its stages world process is the probable realization of **probabilities**possibilities. While the determinist would desire full information, exact to the nth decimal place, on his initial or basic situation, the advocate of emergent probability is quite satisfied with any initial situation in which the most elementary schemes can emerge and probably will emerge in sufficient numbers to sustain the subsequent structure.

6. ...orld process admits enormous differentiation. It envisages the totality of possibilities defined by classical laws. It realizes these possibilities in accord with its successive schedules of probabilities. And, given sufficient numbers and sufficient time, even slight probabilites become assured.

7. Norld process admits break-downs. For no scheme has more than a probability of survival, so that there is for every scheme some probability of a break-down; and since earlier, schemes condition later achemes, a break-down of the former entrains the break-down of the latter.

8. World process includes blind allers. For schemes with a high probability of survival have some probability of emergence. In so far as they emerge, they tend to bind within their routines the possible materials for the possibility of later schemes and so to block the way to full development.

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9. The later a scheme is in the conditioned series, the narrower is is its distribution. For actual realization is

less frequent than its concrete possibility; and each later set of schemes is concretely possible only where earlier, conditioning schemes are functioning.

10. The narrower the basis for the emergence of each later set of schemes, the greater the need to invoke long intervals of time. For in this case the alternative of large numbers is excluded.

11. The greater the probabilities of blind alleys and of break-downs, the xrater greater must be the initial absolute numbers, if the realization of the whole series of schemes is to be assured. For in this case the device of long time intervals might result in no more than a longer sprival of inert, elementary routizes and more numerous fresh starts leading to further break-downs might not be efficacious. Blind alleys with their inert routines could last for extremely long periods and, when they suffered break-down, they might result in another blind alley. Again, a situation which led to some development only to suffer break-down might merely repeat this process more fre uently in a longer interval of time. On the other hand, the effect of large initial numbers is to assure at least one situation in which the whole series of schemes will win through.

12. The foregoing properties of world process are generic. They assume that there are laws of the classical types, but they do not assume the determinate content of any particular classical law. They assume that classical laws can be combined into the circular relationships of schemes, but they do not venture to analyse the structure of any scheme whatever. They assume that there are statistical laws, but there is no assumption of any the determinate content of any statistical law.

Moreover, these properties are relatively invariant. They rest on the scientist's necessary presupposition that there are classical and statistical laws to be determined. But they in no way pre-judge the determination of those laws nor the manner in which they are to be combined to yield schemes of recurrence and their successive probabilities. It follows that the foregoing properties of world process cannot be upset by any amount of scientific work in the determination of classical or statistical laws.

Again, these properties are explanatory of world process. They reveal an order, a design, an intelligibility. For they account, in generic fashion, for numbers and time intervals, for distributions and concentrations, for bland alleys and break downs, for increasing systematization, for stability differentiation, for increasing systematization, for stability without necessity, for assurance without determinism, for development without chance.

Finally, the intelligibility, offered by the explanation, is immanent in world process. It exhibits the inner design of world process as an emergent probability, and from that design it concludes to the outstanding, generic features of the same process. Accordingly, since empirical method aims at such an immanent intelligibility, emergent probability is a view of world order within the limits of empirical method. As we began by inviting the reader to grasp the intelligibility immanent in the image of a cart-wheel, so now we are inviting him to perform again the same kind of act. The only difference is that, for the image of the cart-wheel, he now must substitute the main features of the universe of our experience.

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blacification by Contrast:

3.0 There is a clarification of ideas through contrast with their opposites. As we have argued that an acceptance of both classical and statistical laws leads to some such world view as emergent probability, so now we have to see how different methodological positions result in different world views.

3.1 Aristotle recognized both natural laws and statistical residues. But his natural laws lumped together both work in primitive confusion not only classical laws and schemes of recurrence but also an element or aspect of statistical laws. His distinction was between the necessary and the contingent. The necessary was what always happens, as in the movements of the stars. The contingent was what usually happens; thus, usually, heavy bodies fall to the earth but, some times, they are propped up and so do not fall.

Not only did Arastotle fail to grasp the abstract lawsof nature of the classical type, but explicitly he repudiated the possibility of a theory of probability. For him all canki terrestrial events were contingent. No doubt, effect follows from cause; but it does so, only if some other cause does not intervene; and such intervention is a mere coincidence. The can be traced back to earlier coincidences. It from the earlier coincidences one can regress to still earlier coincidences; but one can never get out of the category of the merely coincidental, and within that category there is nothing to be grasped by any science. Hence, while Aristotle recognized statistical residues and concrete patterns of diverging series of conditions, he had no theory of probability to bring them to heel within the field of scientific knowledge.

Still, Aristotle had no intention of allowing terrestrial process to bog down in a more morass of coincidental interferences. To exorcize such entropy, he argued from seasonal variations to the influence of celestial bodies upon terrestrial activities. Because the sun and moon, the planets and stars, operated necessarily; because they operated from successively different positions; they supplied him with a sufficient ground and cause for the periodicity and perpetuity of terrestrial change. In this fashion there arose his notion of an eternal heaven, an **eternal** earth, and an eternal cyclic recurrence.

Emergent probability differs from the Aristotelian world view, because it rests on a different notion of science and of law. Classical laws are abstract. The alleged necessary movements of the heavens are merely schemes of recurrence that arose through the **EMPANN** unfolding of probabilities and will survive in accord with probabilities. The regularities of terrestrial process are essentially similar, though here the schemes are more complex and the probabilities lower. Finally, stand eternal cyclic recurrence vanishes and in its place there comes the successive realization, in accord with successive schedules of probabilities, of **Exerxmore complex** a conditioned series of ever more complex schemes of recurrence. It is not

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the design of all process; and that design is not an eternal, systexeseness cyclic recurrence, but the realization through probability of a conditioned series of schemes ever more developed schemes.

# The Valileen World View

3.2 Galileo discovered our law of falling bodies, but he failed to recognize its abstractness. Correctly, he grasped that explanation lies beyond description, that the relations of things m to our senses must be transcended, that the relations of things to one another must be grasped, and that a geometrization of nature **trans**, the key tool in performing this task. Still Galileo did not cast his methodological discoveries in the foregoing terms. Instead of speaking of the relations of things to our senses, he spoke of the merely apparent, secondary qualities of things. Instead of speaking of the relations of things to one another, he spoke of their real and objective primary qualities, and these he conceived as the mathematical dimensions of matter in motion.

Thus Galilean methodology is penetrated with philosophic assumptions about reality and objectivity and, unfortunetely, those assumptions are not too happy. Pasy car be traced Their profound influence can be followed in Descartes, in Holdes, bocke, Berkeley, and hume

Their influence is evident in Descartes. Their ambiguities appear in Hobbes and Locke, Berkley and Hume. Their final inadequacy becomes clear in Kant, where the real and objective bodies of Galilean thought kurnank prove to constitute no more than a phenomenal world.

Hitherto, on the other hand, our procedure has been to prescind severely from philosophic questions about reality and objectivity. In due course we shall have to meet them. But our present concern is the fact that Galilean laws of nature are not conceived in abstraction from sensible or, at isats least, imaginable elements and, consequently, that the Galilean law corresponds, not to our abstract classical law, but ration to what we have named a scheme of recurrence the Galilean law stands in the field, not of our abstract classical laws, but rather of our schemes of recurrence in which abstract laws and imaginable elements can combine.

From this concreteness of the conception of natural laws there follows a twofold consequence. On the one hand, there arises the hostility of incomprehension against statistical laws. On the other hand, there results a mechanistic view of the universe. For, in the abstract, classical laws possess universality and necessity. The Galilean acknowledges this universality and necessity but cannot recognize its abstractness. For him, it is attached immediately to imaginable particles or an imaginable ether or both. For him, it is already concrete, and so it is not in need of further determinations to reach concreteness. For him, the further determinations, which would be non-systematically related to one another, simply do not exist. Accordingly, since he has no doubt of the existence of classical laws, he cannot but regard statistical laws as mere formulations of our ignorance. There is some vast aggregate

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of discrete or continuous but imaginable elements; they are subject to universal and necessary laws; and the business of the scientist is the hard task of determining those laws and so predicting what cannot but occur.

Moreover, within this context, the negation of statistical laws involves mechanism. A machine is a set of imaginable parts, each of which stands in determinate systematic relations to all the others. In like manner, the universe, implicit in Galilean methodology, is an aggregate of imaginable parts and each is related systematically to all the others. The sole difference is that, apart from the machine, there are other imaginable elements that can interfere with its operation, but apart from the universe of imaginable elements what imaginable interventions can there arise? Mechanism accordingly becomes a determinism.

Until recently, this Galilean view has been dominant in scientific circles. It easily survived the rather veiled implications of Darwinism. But it seems to have suffered a cripling wound from the overt claims of Quantum Mechanics. Our argument, however, moves on a different terrain. It appeals to Darwinism and to Quantum Mechanics only as illustrations of scientific invelligence. Its proper premises lie in the dya dynamic structure of empirical inquiry and in the canons that govern its unfolding. In that field it has noticed that abstraction is not impoverishing but enriching, that in the sense of enriching abstraction classical laws are abstract, that a systematic unification of classical laws does n t imply the possibility of imaginative synthesis, that the concentration of systematic relationships in the abstract field leaves the further determinations, needed for concrete applications, non-systematically related to one another. It follows that classical and statistical laws, so far from being opposed, are complementary. It follows that the regularities of our universe result, not from classical laws alone, but from the combination of such laws with suitable constellations of concrete circumstance. Finally, it follows that these achmas schemes of recurrence just as the machines that men make merge and function, survive and vanish, in accord with the probabilities successive schedules of probabilities inxaccord for the realization of a conditioned series of schemes.

Closely welsted to mechanism, though distinguishable from it by its most austere formulation, there is a deductivist natical equations. Let us postula te, then, complete knowledge of all these equations and, as well, a perhaps super human dexterity in their manipulation. Then, complete information on any sigle world situation/world istolutor the down matter of all by news c.uld be translated into a debendination of all dr.  $\Theta \hat{a}$ dary conditions and the wooden postulated donterity re. boun world signation. the cose uent deduction of any other wo **ໃ**ນຮອກາ**ດ** 16 61 3.0 Minution to the one RM P ہمہ۔

The divergence between such deductivism and everyent probability seems to me to lie in dissaff the affirmation that one world situation can be deduced from another without any

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3.3 There are those that date the dawn of human Λ intelligence from the publication of Darwin's Origin of Species in 1859. In fact, though the work does not contain any systematic statement of detiodological foundations, it does present the outstanding instance of the employment of probability as a principle of explanation. For, in the first place, Darwinism explaint. The tall, why species differ, why they are found in their observable spetio-temporal distributions, why them numbers in each species increase, or remain constant, or diminish in the second of extinction. In the second place, Metexplanation presents an intellicibility immanent in the data, Frounded in similaridies and differences, in numbers and their rates of change, in distributions over the surface of In the the earth and through the genturies epochs of meology. third place, this immanent intelligibility differs radically from the immanent intelligibility offered, for instance, by Newton's m theory of universal gravitation or Laplace's affirmation of a single mathematical function formula by which a suitably endowed intelligence might deduce any world situation from complete information on a single situation. For the follower of Laplace cannot reach any determinate conclusions, unless he is provided with fully accurate information on the basic situation. But the follower of Darwin is indifferent to the details of his basic situation, and he obtains his conclusions in a second in the second seco by appealing to the natural selection of chance variationsm that arise in any of a warx large veriety of terrestrial processes from any of a large variety of initial situations. It is not difficult to discern in Darwin's natural selection of chance variations a particular case of a move general formula. For it is not the single, isolated variation but rather a combination of variations that is

significant for the evolutionary process. Again, while such combinations of variations may be attributed to chance, in the sense that the biologist is not concerned, with efficient causality, but with an immanent intelligibility, still, what is significant for evolution is the probability of emergence of such combinations of warmations and not the non-systematic divergence from their probability, which is our meaning of the name, chance. Finally, makaralxselection as chance variation is an instance of probability of emergence, so natural selection is an instance of probability of survival. Artificial selection is the work of the breeder, who mates the plants or animals possessing the characteristics he wishes to encourage. Natural selection is the work of nature, which whose a longer life of workanoy and 50 MOVE Prequent Liters to the trees to the tree better onigoed the works of nature, which gaves a shorter life expectancy and so less frequent litters to the typics that are less well equipped to fend for themselves. Still, nature effects this selection, not . ith the/predictability of the changing phases of the moon, but only by a general tendency that admits exceptions and that increases in efficacy with the increase of numbers and the prolongation of time intervals. In a word, natural selection means survival in accord with the probabilities. Moreover, these combinations of variations, which possess probabilities of emergence and of survival,

are relevant to schemes of recurrence. For the concrete living

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of any plant or animal may be regarded as a set of sequences of operations. Such operations are of kinds; there are many of the same kind; and those of the same kind occur at different times. There are, then, in each set of sequences recurrent operations, and the regularity of the recurrence reveals the existence and functioning of schemes.

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Jithin such schemes the plant or animal is only a component. The whole schematic circle of events does not occur within the living thing, but goes beyond it into the environment, from which sustenance is won, and into which offspring are born. No doubt, the higher the type, the greater the complexity and the greater the proportion of significant events that occur within the animal. But this greater complexity only means that the larger circle connects a series of lesset and incomplete circles. The vascular circulation occurs within the animal, but it depends upon the digestive system, which depends upon the animal's capacity to deal with its environment and, in turn, that capacity depends on the growth and nourishment secured by the vascular system.

Again, the plant or animal is a component for a range of schemes. Unlike the planets which stick to their courses in the solar system, and like the electrons which may be imagined to hop from one orbit to another, the plant or animal enters into any of a range of sets of alternative schemes. This range is limited by immanent structure and capacity. Still, though it is limited, it remains open to alternatives. For without change of structure or of basic capacity, the/animal continues to survive within some variations of temperature and pressure, of circumambient water or air, of sunlight and soil, of the floating population of other plants or animals on which it lives.

Further, the probability of the servival of a siven type will depend upon two main factors. On the one hand, where is the face of sets of alternative schemes furthin which the type of animal or plant could function successfully. On the other hand, there is the field of opportunities offered by environment for the functioning of one or more of the alternative sets. There are, of course, further and more complex aspects of the matter but, perkaps, they can be included under the foregoing complex aspects of the matter but, perkaps, they can be included under the foregoing complex aspects of the matter but, perkaps, they can be included under the foregoing complex aspects of the matter but, perkaps, they can be included under the foregoing complex aspects of instance, potentialities for evasion ilight, or self-defence might be added to the schemes in which the animal could function, while competing and predatory animals would be considered as restrictions upon the favorableness of all environment for a given type.

However, if it is true/that living things are involved in schemes of recurrence, one must/not confuse the probabilities of emergence and survival of these schemes/ with the distinct probabilities of emergence and survival of combinations of variations. The former probabilities of schemes regard combinations of events. The letter probabilities of variations regard not events, but potentialities for events. No doubt the two are closely related, for potentialities for events are significant only if the events sometimes occur. Still, even the closest relations in, se far from proving thentity, supreses distinction.

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At this point, however, the differences between Darwinism and emergent probability begin to come to light. Emergent probability affirms a conditioned series of schemes of recurrence that are realized in accord with successive schedules of probabilities. Darwinism, on the other hand, affirms a conditioned series of species of things to be realized in accord with successive schedules of probability. The two views are parallel in their formal structures. They are related, inesmuch as species of living things emerge and function within ranges of alternative sols of schemes of recurrence. None the less, there is a profound difference, For Darwinian probabilities of emergence and survival regard, not schemes of recurrence, but underlying potential composnents for any schemes within a limited range, and the Barwinian series of species is a sequence of higher potentialities that exhibit their development by their canacity to function in ever greater ranges of alternative sets of schemes.

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This difference promots us to recall that the present account of emergent probability did not aim at completeness. We had not raised the question, what are things? We had not determined whether there is an enswer to that question that satisfies the scientific canon of parsimony. Accordingly, we presented emergent probability in the present chapter with the qualification that later, when the notion of thing had been investigated, there might be needed a further development of the analysis.

Darwinism would indicate the necessity of such a further development. Accordingly, if a satisfactory notion of the thing can be reached, there will arise the following questions. Are things potential some components for ranges of schemes of recurrence? Are they variable in these potentialities? Are such variations of potentiality capable of transmission? Is there a series of combinations of transmissible variations of potentiality? Are there the appropriate, successive schedules of probabilities for the emergence and the survival of the series of combinations of transmissible variations of potentiality? Finally, if these questions can be answered affirmatively, can those affirmations rest on general, methodological grounds?

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Complementerity Amplementarity of Cleasured fileh thead missly alm 3. H. Indeterminism. 215) By indeterminism is meast a contemporary tendency that seves its only in to the veryfeel queline of Quantum Mechanics but poes beyond to searce masmuch as it pronunces on the native of a cientific preveled and even mphilosophic issues . While it is offersed radically to mechanical determinism, its positive features do not actual summing description and, perhaps, on pupper will beat be served by descensing encuescuely a serve 1/ canes. Fist as Galileo distinguished between merely appoint secondary punktion and on theother hand, the real and objective dimensions of maker monoton, so too there are ··· indeterminists That offer a comewhat parallel disclosure of the nature of reality. The All destruction between the real and the appearent is retained, but now the real is ~....+ michosofic and random while the merely apparent is the macrosofic mwhich clustical laws come the wenified. However, we mention this usine only to de clone an mimediate descursion. hater in a philosophic context we shell attempt an explanatory account of the abount and less . . . . . . variety of mens on neeling and objectively. For the present we shall have the content with the -----cenor of personing. The scientist only affirm what he can verify and he may not offirm that ~- ~·•• he connor verify Secondly indeterminists tend tragent the old may make putiles and weres and to favour some lyte of conceptual symbolism. Here yain the same is the precise nature of reality but new, by appealing the canon of parcism my we can reach two conclusions. On the one hand it would seem that the only possible were fication of the megned as may mid his in a corresponding sensation; accordingly of the particles are to small and the wave too calle to be enced as particle and waves, then the particles as magined and the were as majoried cannot be verified; and if they cannot the verified they cannot be offermed by the ocentist. On the other hard, it is possible to verify conceptual formelations of they possess sensible implications; for in the meanne that an increasing number and verify of such implication are found to correspond to sensible experience the wind calim of the conceptual formulation is approached. This 0 offecced Relativity is said to be probable not because many scientists feel that They have had a fairly good look at a our- domensional space-time manifold in the came meny scientists working on different problemes have found procedures and predictions pino based on Special Kelting to be highly encoursed. Thirdly there occurs an argument from the her mens I data to the ultimate unverfeability of classical laws. While I do not behave it to be cogent it is well worth allentern. For it appeals & the conterior of veryfielding; it nests in the solid factof the hay incers I date; and it does exclude miscon captions of the nature of classical laws. To begin the hoginess of date is not the denied. What I doil is determinate never is a

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deturn and always is a concept. of themselves data may be said to be determinete materially or potentially; but they become determinete formally only in the measure that they are intremed under art apts; and this proces of subsimption may be prolonged indepriety. This a greater formal determinations of data is possible as long as eccentific concepts can be recursed to guld more presults objects for measurement and as long as a curtific technywiscan be improved to make measurements more accurate. But as hory as a greater fromal determinations is possible, the determinations that actually is atterned is conjoined with an unspeafed remainder of marchy potential determinations That unspecified remainder is the haginess of dute, and it will be with us as long as ner comptional more accurate measurements are possible. Aprevent the hay mens of data alone cannot from the mountichale for clease of laws. Logkally it is I mpossible for a valed an church toritan a here that does not appear on the premises. More an cretely it could be true that whenever date became more determinate formally, new classical laws were descovered, and had that everting class cal laws were always due to be reversed in fever of other classical laws in the present of the classical laws were always due to be reversed in fever of other classical Kans. the comes closer to the case when one argues that classical laws are conceptut formalations, that they process all the determination precision and formal determinationers of concepts that they cound the stripped of that precision and deleminations without cooring the classical laws. In contrast, data are meducally hapy. Because measure ments are never can be accurate to n de comel delaces, where n is a laye as one please classical lens can never he more that then approximative. There essential determinery is more head complet with the hoy mais of data; and so classical laws and reality unverficille. Now thes or ment is walled of classical leave are interfrieted concretely. For on concrete det interpretation classical laws are supposed to tate relations between date & helween elements in this correspondence with date. But the canot he completely determinate relations between excentially have jund es a concrete interpretation classical laws must be my and as no more than approximature. Attle them is no need to integrined classical laws concretely. They can be statements of elements in abstract system where 1) The abstract system is constituted by implicitly defined relations and terms 2) the abstract system is comeched that With date not difectly but through the mediation of a complementary set of descriptive concepts and

3) the lease of the abstract system are said to be weighed masninch as they assign limits

on which, other things being quel, wast verseties of data converge. On this change the

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completely determinate relations of classic cal laws are between the completely determinate terms they implicitly define. This closed structure is referred that through a set I descriptione and to approximative concepts. Finally, the closed structure is proved relevant to date, not by exact coincidence, but by assigning the limits on which date converse. converge.

Furthy the affirmation of convergence is also an admission of duregen u. Sont that admission equivalent to the statement that ultimately clossical laws are not verificable? Again, the issue is the precise nature of verification. It hardly would be classed that any service law was not verified because it did not account for the whole of our experience. But what can hall for service that the classical laws are not the whole laws. The existence of the divergence proves that the classical laws are not the whole of any explaination buildge. But though they are not the whole, they can be aport; and the classical laws that in fact are such a part are the true that are verified in the sense that they assay the limits on which date do converge.

Fifthly it is claimed that Quantum Mechanics is the more peneral them and that it moludes, bey, newtonian & nechanics as a particular case. Here I would suggest the relevance of a distinction between logical inclusion and concrete application. Sier no reason for disputing the contention that Schrödinger's time equation can plausely be completied into newton's second law of sustein. But it need not fallow that the shiplification has no analogue in the world of events. In the contrary it would seem that such an analogue would ever if schemes of recurrence were realized prefectly; and in that case it usual even difficult to maintain that the accuracy A223 of besic observations was not the sale limit to the accuracy of predictions. More headsticilly, in cofer as achimes are not realized perfectly & pifest realy atim cannot the accertanded, at least the near for objective divegetions or subjective ignorance would he assigned

Lichtly, it may be aqued that debennenim aunt the true or false and that we seem to be dadging the same. But if the disg and time is admitted, one finds mealfford interphilic questions. At least in the present context, and contention well be that the old determinism with its philosophic implecetions has by one way to new panely seeked object view that converses in a developing anticipation of a deterministerly set. Such a way would remain with in the timets of amplicial science of would distinguish between an anticident component of methodological science of would consequent component of probably verified laws and provide a complication and a consequent component. The anticident component develops; mitally it consists in such a verified. The anticident component develops; mitally it consists in consequent component. The anticident component develops; mitally it consists in such very periodities as the anticident component develops; mitally it consists in such very periodities as the anticident that there is a reason for every thing; subsymethy, as a verified adverses, it lakes on the increasing precision fever more accurately.

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Complementer differentieted hervestic structures again, the consequent conforment is subject to valiation, for what is reporded as veryfied at any time may be celled not give time and subjected to revesion. He concrete conjunction of the two components in the muds of scientists constitute about time their anticipations of a determinate object; and When the components are undergoing profound change, there naturally will be some uncertainty in their anticipations! On this were the old deleminism was sustation not only because it was muchued in Philosophie is sness lint also because it fulled to envice a the fourthely mat Adevelopment in Lewistic structures. It supposed the universal validity of a lyte " Desplanation that is possible only when schematic situations are needing of perfectly. Atombodid the possibility of a type of captanation in which the probabilities of the non-schematic account fil the emergence of the schematic. Indeleminesin's frue as a negation of the old deleminism Bat it cannot escape the necessary of methodological assumptions and precepts it cannot prevent their conjunction in They H- with laws and prequencies that are no added as very cid; and so it cannot even in deleging the day when, from a new weepoint scientific anticipations once more will enviry a a deleminate type of the known. Hence at the present time, there is some difficulty in ope up in in a muersally acceptable feshion just what is the determinate of objiel-that science is tasticipate. a chident of himon browledge can make cay estim that repard The onleadent and non- go tematic without a unified when that anticipales both mayht into concrete non-schematic situations. The persibility Concrete may ht mts the non-achematic situations of the sub-atomic order probably well be called integration on both practical and themetical prounds. Havene I do not propose balocuss this as feet of the same principally became it regards the consequent component of methodological anticipations, hut also be cause I believe all discussions of concrete possibility & suffer forme radical ambey with for many monete usine further nicipht waling possible and when it occurs whatpreviewsly seemed impossible turns out the pute feasible off wall. C

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3.4 Nineteenth century physicists were prone to regard Darwinism as the triumph, in the field of biology, of their own mechanistic view of world order. So far from suspecting that a new type of scientific explanation had been introduced, they took it for granted that Darwin's chance variations were but another name for mechanical processes too complex to be statedim in detail. In this fashion the crisis in the world view,

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In this fashion the crisis in the world view, immanent in scientific methodology, was postponed from the nineteenth century to the twentieth. It fell, not to biology, but to the invasion of physics itself by Relativity and by Quantum Mechanics, to force a radical revision of scientific outlook. Moreover, since the immediate result of a crisis is that the old thesis gives way, not at once to a higher synthesis, but rather to a set of merely contradictory antitheses, contemporary opinion tends to be content to replace determinism by indeterminism and mechanistic imagery by some symbolicism.

3.41 Inasmuch as indeterminism arises before imagery as such is attacked, the tendency is to replace one picture of the universe by another. There had been the picture of a vast aggregate of very small knobs, each centered at a pointinstant and each subjected to a set of forces; moreover, it was believed that, in principle, the coordinates of position and the magnitude and direction of the forces were determinable to n decimal places with n as large as anyone pleased. There has risen an antithetical picture of a vast aggregate of, say, wavicles that can be located only approximately and that respond to accretions of energy, now in one manner, and now in another.

The canon of parsimony makes short work of both pictures. The scientist can affirm what he can verify. Directly in experience he can verify experiential conjugates. Indirectly, in combinations of experiences, he can verify pure conjugates. But there is no rhyme or reason to the view that either in experiences or in combinations of experiences he will ever verify pictubes of what is too small to be seen. xhxkxisxwerified;xis;ahwaysxaxformulations

The only way in which a picture can be verified is to see or hear, taste or touch or smell, precisely what is imagined. Such verification is not possible in the realm of the sub-acomic. Therefore, pictures of the sub-atomic lie outside the realm of possible empirical science and must be left to artists and journelists.

**5.41** However, one can admit this **indeter** application of the canon of parsimony and still affirm an indeterminism, not indeed of pictures of the infra-sensible, but of the data that actually are sensed. Geometrical images endeavorss to take on the properties of geometrical concepts; the image of a point has magnitude but the concomitant concept denies it magnitude; the image of a line has breadth, but the concomitant concept denies it breadth. By ding of imagining ever smaller points and ever thanner lines, the geometer generates in himself the illusion that his images possess the accuracy of his concepts and, moreover, when he turns his mind to physics, he fancies a universe with positions and forces accurate to any number of decimal places. Still, while the principle of excluded middle would necessitate the conclusion that **the i** 

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next decimal place must be occupied by a 0, or a 1, or a 2, etc., it remains that human senses, how matter how delicate the instruments that extend their range, must eventually meet their Waterloo and be forced to answer that further decimal places are indeterminate.

To take another instance, what to me is just a bug, to an entomolocist is an dnimal that falls with neat precision under a series of differentiations. Both of us look at the g bug, but I see only a slight fraction of what he accurately observes. He could point out to me, one by one, the features that I do not notice. In each case I could be brought to see the aspect or quality to which he draws my attention. Still, he would not have gone very far before I would begin to forget my earlier lessons and fail to distinguish between features already noticed and features under present scrutiny. In other words, the observation of data is not a mere matter of looking. To become a trained observer in any field, one must ac uire a range of conceptual categories that both guide mar seeing systematically through a series of centers of attention and, as well, hold in synthesis the set exact set of aspects that successively fall under observation. Now, if this is so, there arises an obvious extrapolation. Future scientific development will bring ever fuller and more accurate categories of classification and description, and so future observations will stand to present observations by trained scientists, as their present observations stand to the looking without noticing of mere laymen. It follows that, at every stage of scientific development, data have no more than an incomplete determinacy and, beyond that determinacy,

there lies an indeterminacy. New, I believe the fore-oing contentions to be, in the main, correct. But it would seem that some distinction has to be drawn between the indeterminate and the determinable. For, while neither is actually determined, still the indeterminate cannot be determined, and the determinable is what can be determined.

Moreover, there is may be assumed to be a series of future stages of scientific development, and in each of these stages except the last, if there is a last, there will be data, not actually determined yet determinable. For in the next stage with its better instruments and its fuller complement of more accurate categories, more decimal places will be settled and more data will meet with effective attention.

At once it follows that, in any stage of scientific development except the last, one cannot draw the line between the inheterminate, which cannot be determined, and the determinable, that can and will be determined. around the luminous area of determined data, there is a penumbra of determinable data; and only around that penumbra of unknown extent, is there the full darkness of the indeterminate.

Further, at each stage of scientific development, scientific intelligence abstracts from the data to which it does not advert. If so far as these data are determinable, the abstraction is an oversight that will be corrected in later stages of development. But in so far as these data are indeterminate, they never can influence scientific understanding, and so just be counted among the merely empirical residue of data from which intelligence slways abstracts. In other words, the indeterminate is also insignificant. Beyond the decimal places that today are settled,

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3.43 However, while I would not object to a claim that there exists an irreducible haziness to data, I think considerable care must be exercised in drawing inferences from this fact.

First of all, this haziness cannot affect the content of any science at any time. To establish laws, it is enough to show that they satisfy actual observations and actual measurements. To refute laws, there is no use appealing to observations and measurements that never can be made. One has to produce the evidence, and the evidence always consists in the determinate content of actual observations and actual measurements.

Secondly, this haziness is not surprising to anyone that grasps abstraction to be not impoverishing but enriching. here resident to preside the president to be and the president to be and the president to be a straight to be a

If one supposed that laws relate sensible contents, one would be confronted with the dilemma either of denying the haziness of data to save the precision of the laws or else of denying the precision of the laws to save the haziness of the data. But, in fact, laws relate, not sensible concents, but abstract conjugates that implicitly are defined by the laws themselves. For laws are reached and are verified, inxeam not in data, but in combinations of combinations of combinations of data; and the meaning of the law is, not the concrete combinatory structure, but only its abstract pattern. Thus, every law is a general formula; to move from the law to the concrete, there must be added further information assigning particular numerical values to specific variables; and sexthenian the haziness of data implies that this further information cannot be completely accurate; but this defect of accuracy in the further information for the law//does not necessarily impuen the validity of the law; ////c/ can be the completely accurate limit on which all actual observations and measurements converge.

Dremencs converge.

Thardly, it follows that the shift from the old data thesis of determinism to the more antithesis of indeterminism rests on an unconscious pr assumption that abstraction is impoverishing. For, as we have just seen, the haziness of data does not mecessity necessitate any denial of the complete accuracy of classical laws in the abstract, where, however, abstraction is supposed to be enriching. But, as we have also seen, shen absuraction is supposed to be impoverishing, then laws relate denuded replicas of aspects contained in data. The meaning of the law is not constituted ultimately by understood relations implicitly defining/terms and, inversely, kerms conceptual terms fixing intelligible relations. The meaning of the law includes a reference to a totality of instances, where each instance is a part or component or aspect in the sensibly given. On that showing, the law is concrete so that either laws must be inaccurate or else data must be as determinate as concepts.

Fourthly, the notion of enriching abstraction does, of course, raise a problem on the nature of objectivity. If the meaning of laws is constituted by understood relations implicitly defining terms, one cannot say that this meaning is objective in the sense that it is something out there to be looked at with one's eyes. Still, within the present context, it is not the notion of enriching abstraction but the development of science itself that creates this problem of spinstively objectivity;

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and, again within the limits of empirical science, an answer to the problem is supplied by the canon of parsimony. For the simple-minded notion that the objective is what is out there to be looked at, constitutes the vulnerable point both in Galileo's primary qualities and in Newton's true motion. Galileo maintained colors and sounds and the like to be measly subjective; he affirmed as real and objective the geometrical dimensions of matter in motion. Again, Newton considered movements relative to observable bodies to be apparent and movements relative to absolute space to be true. Still, operating within the field of empirical science, Einstein decided to treat viven extensions and durations in the same fashion as Galileo treated colors and sounds; and when he did so, he//efected a space and time that, whatever their objectivity, are not "obyiously out there to be looked at." Finally, as there is a canon of complete explanation to cover the Einsteinian prodedure, so also there is a canon of parsimony to account for the validity of abstract laws. As the scientist is not entitled to affirm what he cannot verify, so he is entitled to affirm what he can verify; but classical laws are verifiable, for verification consuit consists, not in your layman taking a good look, but in schentists interpreting the combinations of combinations of combinations of

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thousands of particular results attested by trained observers. Fifthly, there follows a judgment on the view that classical laws are mere macroscopic approximations to microscopic realities. Obviously, there is no objection to such an account of some classical laws, such as the formula nelating the volume, pressure, and temperature of a cas

Fifthly, there follows a judgment on the view that all classical laws are mere macroscopic specialities. approximations to microscopic realities. Just as the formula relating the volume, pressure, and temperature of a gons gas is a statistical result of random movements, so also, some would claim, the law of inertia draws a merely ideal line about which moving bodies oscillate at random but imperceptibly. Now, clearly,/Simrigraisariy/if the oscillations are/imperceptible, they are unverifiable; and if they are unverifiable, they can be affirmed not by scientists but only by journalists and poets. Again, if classical laws are verifiable, what more can be needed or wanted for their validity? There is no scientific need, but only an extra-scientific im itch for an image of what really is going on "out there."

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4. Let us bring this long chapter to an end. It began from the problem of apparent duality that arose from the existence of two types of insight, two heuristic structures, and two distinct methods of empirical investigation. There was no question of eliminating the duality, for the direct and the inversed types of insight both occur. There remained, then, the task of relating diverse procedures and results into a single whole. In a first section it was argued that classical and statistical investigations are complementary as cognitional activities. In a second section it as revealed how their results, whatever their precise content, can be combined into a single world view. In a third section thus world view was contrasted with the Aristotelian, with that of mechanist determinism, with the Darwinian view, and with contemporary tendencies to affirm an indeterminism. In the course of the argument the problem of the thing and, with it, the problem of objectivity became increasingly apparent. But before tackling such large issues, it will be well to broaden the basis of our ap operations and so we turn to the notions of space and time.

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